

Adapted from Graham's lecture slides.

第一章：概论

函数，函数式程序设计，
历史回顾，Haskell的特点和例子

函数

- In Haskell, a function is a mapping that takes one or more arguments and produces a single result.

```
double x = x + x
```

- Computation by function application

```
double 3
= { applying double }
  3 + 3
= { applying + }
  6
```

- Computation by function application

```
double (double 2)
=   { applying the inner double }
double (2 + 2)
=   { applying + }
double 4
=   { applying double }
4 + 4
=   { applying + }
8
```

- Computation by function application

```
double (double 2)
=   { applying the outer double }
double 2 + double 2
=   { applying the first double }
(2 + 2) + double 2
=   { applying the first + }
4 + double 2
=   { applying double }
4 + (2 + 2)
=   { applying the second + }
4 + 4
=   { applying + }
8
```

函数式程序设计

- Functional programming is style of programming in which the basic method of computation is the application of functions to arguments;
- A functional language is one that supports and encourages the functional style.

例子

Summing the integers 1 to 10 in Java:

```
int total = 0;
for (int i = 1; i ≤ 10; i++)
    total = total + i;
```

The computation method is variable assignment.



Summing the integers 1 to 10 in Haskell:

```
sum [] = 0
sum (x:xs) = x + sum xs
sum [1..10]
```

The computation method is function application.



历史回顾

1930s:



Alonzo Church develops the lambda calculus, a simple but powerful theory of functions.



历史回顾

1950s:



John McCarthy develops Lisp, the first functional language, with some influences from the lambda calculus, but retaining variable assignments.



历史回顾

1960s:

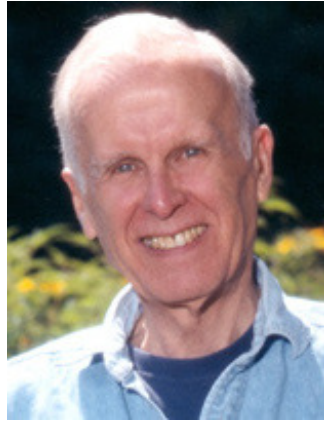


Peter Landin develops ISWIM, the first *pure* functional language, based strongly on the lambda calculus, with no assignments.



历史回顾

1970s:



John Backus develops FP, a functional language that emphasizes *higher-order functions* and *reasoning about programs*.



历史回顾

1970s:



Robin Milner and others develop ML, the first modern functional language, which introduced *type inference* and *polymorphic types*.



历史回顾

1970s - 1980s:



David Turner develops a number of *lazy* functional languages, culminating in the Miranda system.



历史回顾

1987:



An international committee starts the development of Haskell, a standard lazy functional language.



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历史回顾

1990s:

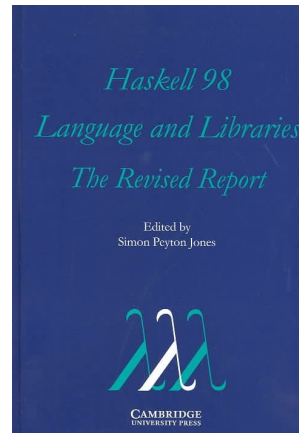


Phil Wadler and others develop *type classes* and *monads*, two of the main innovations of Haskell.



历史回顾

2003:



The committee publishes the Haskell Report, defining a stable version of the language; an updated version was published in 2010.



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历史回顾

2010-date:



Standard distribution, library support, new language features, development tools, use in industry, influence on other languages, etc.



Haskell的特点

- 简洁（声明式）：第2章，第4章
- 强有力的类型系统：第3章，第8章
- List comprehensions: 第5章
- 递归函数：第6章
- 高阶函数：第7章
- 表达副作用的函数：第10章，第12章
- Generic函数：第12章，第14章
- 惰性计算：第15章
- 程序推理：第16章，第17章

例1: 序列求和

$$\begin{aligned} \text{sum } [] &= 0 \\ \text{sum } (n:ns) &= n + \text{sum } ns \end{aligned}$$
$$\begin{aligned} &\text{sum } [1,2,3] \\ &= \{ \text{applying sum } \}'' \\ &1 + \text{sum } [2,3] \\ &= \{ \text{applying sum } \} \\ &1 + (2 + \text{sum } [3]) \\ &= \{ \text{applying sum } \} \\ &1 + (2 + (3 + \text{sum } [])) \\ &= \{ \text{applying sum } \} \\ &1 + (2 + (3 + 0)) \\ &= \{ \text{applying } + \} \\ &6 \end{aligned}$$

例2: 快速排序

```
qsort [] = []
```

```
qsort (x:xs) = qsort ys ++ [x] ++ qort zs
```

where

```
ys = [a | a ← xs, a ≤ x]
```

```
zs = [b | b ← xs, b > x]
```

例3: 序列求“和”一般化: 高阶函数

$$\begin{aligned} \text{sum } [] &= 0 \\ \text{sum } (n:ns) &= n + \text{sum } ns \end{aligned}$$

$$\begin{aligned} \text{foldr plus zero } [] &= \text{zero} \\ \text{foldr plus zero } (n:ns) &= \text{plus } n (\text{foldr plus zero } ns) \\ \text{sum} &= \text{foldr } (+) 0 \end{aligned}$$

练习: 用foldr定义 (1) 计算数字列表的乘积; (2) 计算列表的长度。

例4: 生成无限序列

```
cyclic = let x = 0 : y  
          y = 1 : x  
          in x
```

```
ns = 0 : foldr f 0 ns  
    where f n r = (1+n) : r
```

作业：

【1-1】 Define a function *product* that produces the product of a list of numbers, and show using your definition that $product [2,3,4] = 24$.

【1-2】 Define list reverse function using *foldr*.

【1-3】 How should the definition of the function *qsort* be modified so that it produces a reverse sorted version of a list?